

## Exercise #7

(範圍: Rings, Groups)

1. Prove (b) and (e) of the theorem on page 142 of lecture notes. (15%)
2. Prove the theorem on page 146 of lecture notes. (20%)
3. P. 685: 12 (only for (b)). (20%)
4. Prove that in  $Z_n$ ,  $[a]$  is a unit if and only if  $\gcd(a, n) = 1$ . (15%)
5. P. 704: 4. (15%)
6. Solve  $x \equiv 8 \pmod{11}$ ,  $x \equiv 9 \pmod{12}$ , and  $x \equiv 10 \pmod{13}$ . (15%)